## B.C.A. Ist Semester Examination, 2021-22

## Paper - III

## [Mathematical foundation of Computer Science]

## Paper Code- BC-153

Time : 2:30 Hours] [Maximum Marks : 70

Note: Attempt any five question. All question carry equal marks.

- 1. (a) Obtain the principal conjunction normal form of  $(P \to Q) \wedge (Q \to R).$  7
  - (b) Show that the given relation R on the set of Real Number is an equivalence relation, which is defined by.

 $(p,q)R(r,s) \Rightarrow (p+s) = (q+r)$ 

2. (a) Solve the recurrence relation  $a_n=5a_{n-1}-6a_{n-2}$  Where  $a_0=1$  and  $a_1=4$ 

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- (b) Using mathematical induction, prove that the following statement is true for all positive  $integer\ n.\ 1^3+3^3+5^3+\cdots+(2n-1)^3=n^2(2n^2-7)^3$ 
  - 1) for n>=1.
- 3. (a) Evaluate f(3) given that  $f(x)=|x-6|+x^2-1$  7
  - (b) State and prove Lagrange Theorem.
- (a) Explain the two type of quantifier with example. 7
  - (b) Show that  $R \wedge (P \vee Q)$  is a valid conclusion from the premises  $P \vee Q, Q \rightarrow R, P \rightarrow M$  and  $^{\sim}M$ .
- 5. (a) Draw the Hasse Diagram of all possible subsets of set A={1, 2, 3}. https://www.sdsuvonline.com 7
  - (b) Show that every Right or Left Coset in a Group are either identical or Disjoint.
- 6. Write short notes on:
  - (i) Complemented Lattice

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- (ii) Cyclic Group
- (iii) Anti Symmetric Relation
- (iv) Recursive Funtion
- 7. (a) Prove that 11<sup>n+2</sup>+122<sup>n+1</sup> is divisible by 133 by

  Mathematical induction for n>=1.
  - (b) Let R be a relation on set A={1, 2, 3, 4} defined by

 $R=\{(1,2),(2,3),(4,3),(4,1),(1,4),(4,4)\}$  find the : 7

- (i) Reflexive Closure of R
- (ii) Symmetric Closure of R
- (iii) Transitive Closure of R

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